Differential Camera Tracking through Linearizing the Local Appearance Manifold

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Abstract

The appearance of a scene is a function of the scene contents, the lighting, and the camera pose. A set of n-pixel images of a non-degenerate scene captured from different perspectives lie on a 6D nonlinear manifold in $\Re^n$. In general, this nonlinear manifold is complicated and numerous samples are required to learn it globally.

In this paper, we present a novel method and some preliminary results for incrementally tracking camera motion through sampling and linearizing the local appearance manifold. At each frame time, we use a cluster of calibrated and synchronized small baseline cameras to capture scene appearance samples at different camera poses. We compute a first-order approximation of the appearance manifold around the current camera pose. Then, as new cluster samples are captured at the next frame time, we estimate the incremental camera motion using a linear solver. By using intensity measurements and directly sampling the appearance manifold, our method avoids the commonly-used feature extraction and matching processes, and does not require 3D correspondences across frames. Thus it can be used for scenes with complicated surface materials, geometries, and view-dependent appearance properties, situations where many other camera tracking methods would fail.

1. Introduction

In this paper we address the challenging problem of tracking in scenes with highly view-dependent appearances. For example, scenes with curved reflective surfaces, semi-transparent surfaces, and specular reflections all change in appearance as the viewpoint changes. This confounding behavior typically makes motion estimation very difficult.

Traditionally, tracking is formulated as a search problem in the parameter space of the transformation. Almost all tracking approaches use an invariant or parametric model of the scene appearance. There are two main classes of tracking approaches. The first class selects a number of salient features and employs them as an invariant model of the scene. The second class extracts the tracking information from all observations.

Lounget-Higgins [13] employed selected salient features and their motion in consecutive frames to compute the epipolar geometry. The epipolar geometry then delivered the relative camera motion of a calibrated camera. This method was later extended to general cameras [15, 14].

Methods that use all observed pixels are often applied in differential settings. Optical flow based methods are employed to simultaneously recover structure and motion [3, 10, 8]. These methods rely on a constant appearance of the scene or a known parametric representation that can accommodate the varying scene appearance. This second class of techniques is more closely related to our technique, which also uses all the image information concurrently. For example, the appearance of an object under different lighting conditions is represented as a 3D illumination linear subspace in [7, 4]. Bascle and R. Deriche modelled the appearance of an object using texture appearance templates [1]. A parametric representation of the scene can also be formulated as a global statistics of the objects' appearance [2, 5], or a filter response [12]. Given the appearance model of the object, a nonlinear estimation framework is used for tracking [2]. Recently, Elgammal proposed to learn a generative appearance model of an object offline, and employ the model to compute the geometric transformation given the change of the appearance [6].

In this paper, we present a method that tracks the camera motion through linearization of the local appearance manifold. A camera cluster with small baselines is used to acquire local appearance samples. Then these samples are used to compute a linear approximation of the local appearance manifold and to estimate the camera motion parameters in this linear space. Our proposed method does not require any 3D or 2D correspondences, thus it accommodates scenes with view-dependent appearance variances. In contrast to the methods based on learning an invariant appearance representation, our method avoids the learning process that requires training data.

2. Problem statement

Our novel tracking approach targets scenes with highly view-dependent appearances. As far as we know this class of scenes is not handled by any existing technique. It is very difficult to model appearance behavior in general, and for this specific class of scenes it is particularly hard to find a *global* model due to the highly nonlinear appearance function. Instead we use multiple *local* models that represent the global manifold about the current viewpoint. These local models are concurrently extracted from the scene while performing the tracking.

Consider a camera that undergoes complete 6D motion (3D translation and 3D rotation) in a static scene. At each frame time, it captures from its current pose P an n-pixel intensity image I of the scene. Each appearance sample I represents a point in a high-dimensional space $\Re^n$. As the camera changes its pose P, I also changes, moving along a manifold in $\Re^n$. One can see that there exists a mapping from P to I, denoted as $I = f(P)$. Since the transformation space of the camera pose has six degrees of freedom, the dimensionality of the appearance manifold is at most six. The dimension will be smaller for cases of degenerate camera motion—for example it will have dimension three for pure translation. For degenerate scenes the dimensionality of the appearance manifold can be less than six. For example, when a camera looks at a very distant scene f is not invertible and the motion can not be fully recovered. In this paper, we consider only cases where the appearance manifold is not degenerate, and accordingly f is invertible.

In general the appearance manifold of a scene is highly nonlinear. Accordingly, numerous samples need to be acquired to learn a representation of it. Although learning f globally would be an ideal solution, this task is mostly infeasible in practice due to changes of lighting conditions and movements of scene objects during capture, which violate the static scene assumption. However, as discussed above, we know that the dimensionality of the appearance manifold is at most six. Hence, a small number of appearance samples simultaneously captured around current camera pose are enough to derive a local approximation of the appearance manifold. In particular, with six samples one can generate a linear approximation of the appearance manifold as $dI = FdP$, where dI is the difference image, dP is the camera motion, and F is the Jacobian matrix. This holds as long as the camera motion is within the range of an acceptable linear approximation. To achieve our goal we need to solve three fundamental problems:

1. How to capture local appearance samples?
2. How to derive a local linear approximation given appearance samples?
3. Is a linear approximation is sufficient?

We will address these problems in the following sections.

3. Tracking

This section introduces our novel tracking frame work. We will discuss how our techniques locally approximates the appearance manifold with linear functions and introduce a technique to capture the appearance manifold while the tracking.

3.1. Linearize the appearance manifold

In this section, we introduce the algorithm to linearize an appearance manifold and track camera motion inside the linear space. Assume at time t, we simultaneously acquire a center image I_0 from current camera pose P_0 and m perturbed images I_k at nearby perspectives P_k ($k = 1, \ldots, m$). Thus we can compute m difference images dI_k and camera motion dP_k by subtracting I_0 and P_0 from I_k and P_k. We want to use these samples to linearize the appearance function $I(P)$ around P_0:

$$I = I_0 + F\,(P - P_0) \tag{1}$$

$$dI = F\,dP. \tag{2}$$

Here I and dI are n-pixel images represented as $n \times 1$ vectors, P and dP are 6×1 pose vectors, and F is the Jacobian (partial derivative) matrix $\partial I / \partial P$ of size $n \times 6$. As m samples of dI_k and known dP_k are acquired, we can combine these sample vectors into matrices and write the linear equation as:

$$[dI_1, dI_2, \ldots, dI_m] = F\ [dP_1, dP_2, \ldots, dP_m] \tag{3}$$

If m is greater than 6 and the images and poses are not degenerated, the equation is of rank 6. We can compute the least square solution of F using the Moore-Penrose pseudo inverse as

$$F = [dI_1, dI_2, \ldots, dI_m]\ [dP_1, dP_2, \ldots, dP_m]^{+} \tag{4}$$

The above discussion addresses the appearance manifold linearization problem in the general case where $m \geq 6$. For an efficient system, one would like to use minimum number of perturbed cameras whose poses expand a 6D motion space. In this case, $m = 6$ and the Jacobian becomes

$$F = [dI_1, dI_2, \ldots, dI_6]\ [dP_1, dP_2, \ldots, dP_6]^{-1} \tag{5}$$

Once a linear approximation is derived for the local appearance manifold, we can estimate the camera motion using a linear solver. Assume at frame $t + 1$, an updated center image $\tilde{I}_0$ is captured at the new camera pose $\tilde{P}_0$, and a temporal difference image $d\tilde{I}_0$ is computed by subtracting I_0 from $\tilde{I}_0$. We can then estimate the camera motion $dP = \tilde{P}_0 - P_0$ as the least square solution of Equation (6).

$$F\,d\tilde{P} = d\tilde{I}_0 \tag{6}$$

3.2. Sample with a camera cluster

As shown in Fig. 1 we have constructed a prototype *differential camera cluster* consisting of four small synchronized and calibrated cameras: one *center* camera C_0 and three cameras C_1, C_2 and C_3 that are offset from the center. The coordinate frame of the cluster is defined to align with the center camera. We call the other three cameras C_1, C_2 and C_3 *translational* cameras as they capture images from translated viewpoints.[1] At any point in time, the *center* camera and the *translational* cameras can be used to obtain four simultaneous appearance samples of the local appearance manifold. See the example images indicated by the green arrows in Fig. 1. In addition we generate three warped images by rotating the image plane of C_0 around its three coordinate axes. See the example images indicated by the red arrows in Fig. 1. One can consider these warped images as having been captured by three virtual *rotational* cameras C_4, C_5 and C_6, each with the same camera center as C_0 but with rotated axes. Thus at any frame the cluster effectively "captures" seven local appearance samples $I_0, \ldots, I_6$. In a non-degenerate case these seven images can be used to derive a first order approximation of the local appearance manifold.
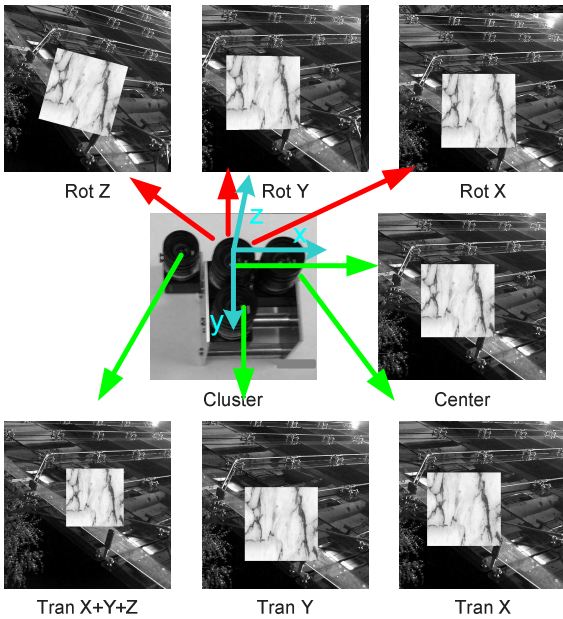

Figure 1. A prototype *differential camera cluster* (center) and illustrative images. We obtain seven images total: one center, three translated, and three rotated. Note that the images shown above were rendered with an exaggerated baseline to make the differing perspectives more apparent.

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[1] In a general case, their axes do not need to be parallel with those of the *center* camera.

The camera cluster provides seven real-time appearance samples. Because the *rotational* images are warped versions of the *center* image, the four samples are from the same manifold. However, the *translational* samples are captured using different cameras. To use these samples for linearizing the local manifold captured by the center camera, we need geometric and photometric consistency across cameras. Assuming the radial distortion is removed from all cameras, we can achieve geometric consistency by using the *intrinsic* parameters of the *center* camera for the *translational* cameras. Specifically we decompose the projection matrix [9] to obtain camera intrinsic and extrinsic parameters. We then generate three virtual *translational* cameras using the *intrinsic* parameters of the *center* camera and the *extrinsic* parameters of the real *translational* cameras. We then generate the translational images using homography mappings. To ensure photometric consistency across the cameras we used the approach presented in [11]. The approach consists of a closed-loop process that tunes the camera hardware settings such that the colors values of a 24-sample color target are consistent in all camera images. This is followed by a software post-processing step that uses the same 24 color samples to compute a mapping that further improves photometric consistency.

4. Linearity of the local appearance manifold

4.1. An SVD analysis

In theory, given six non-degenerate samples one can always generate a linear approximation of the appearance manifold, but such a linearization is accurate only within a limited region. The size of each locally-linear region is determined by the local smoothness of the manifold. Typically, the scene appearance is a highly nonlinear function and its locally-linear regions are quite small. This means that any differential camera cluster should have very narrow baselines and a very high frame rate to acquire samples and restrict motions within a small locally-linear region. This is a great challenge. Even if these requirements can be satisfied, due to the inherent electronic noise of the camera, the signal-to-noise ratio of the spatial and temporal difference images might not be big enough to recover motion accurately. We try to alleviate this problem by blurring the images to smooth the appearance manifold.

Let us examine the smoothness of the appearance manifold for a synthetic 3D scene consisting of two textured planes (see the images in Fig. 2). The two planes are placed at different depths to help distinguish the parallax effects from out-of-plane rotation and in-plane translation. Several rectangular white textures are pasted on the dimmed background (around the periphery) to provide some low frequency texture the scene. The resolution of the synthetic camera is $n = 640 \times 640$. As shown in Fig. 2(a), we use a

uniform distribution to randomly perturb the camera pose and generate $m = 50$ images from nearby perspectives. The maximum magnitude of the perturbation is carefully defined so that the imaging of a point on the frontal plane shift at most 4 pixels away from its position in the center position. The images are blurred using a Gaussian filter and sub-sampled at a 4-to-1 rate (see Fig. 2(b)). This sampling rate is higher than the Nyquist rate. We then acquire difference images by computing a mean image and subtracting it form the sub-sampled images. The pixel intensities of these difference images are reordered into column vectors and grouped into a $n \times 50$ matrix. We then apply SVD decomposition to the matrix.

To demonstrate the effects of smoothing the appearance manifold, we use three different Gaussian kernels of size $[20 \times 20, 40 \times 40, 80 \times 80]$ and $\sigma = [3, 6, 12]$ to filter the original perturbed images and generate three sets of blurred images. The SVD results on matrices constructed using these blurred images are shown in Fig. 2(d,e,f). One can see from Fig. 2(e,f) that there are six significant singular values, which implies that the smoothed local appearance manifold can be appropriately linearized and the motion can be recovered. While in Fig. 2(d), the fourth, fifth and sixth singular values are not easily distinguished from the rest. While in general this could be an indication of a degenerate scene (under-constrained), in this case it is an indication that there is considerable non-linearity embedded in the appearance manifold for the region where the samples are captured. To address this we can sample closer to the center pose, or smooth the images more heavily.
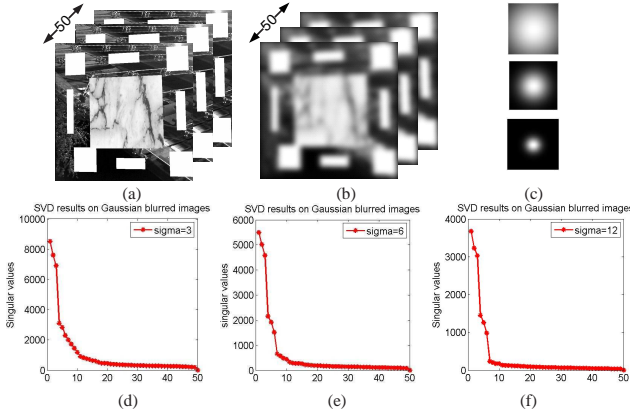

(a) (b) (c)

(d) (e) (f)

Figure 2. SVD analysis using synthetic images of a 3D scene with textured foreground and background planes. The foreground plane is the marbled square in the middle of the images. (a) The original images captured from 50 close perspectives. (b) The blurred images. Three Gaussian filters with $\sigma = [3, 6, 12]$ are used. (c) The power spectrum of the three Gaussian filter within $[-40, 40]$ of the frequency domain. (d) (e) (f) SVD results using the three different filters.

4.2. A quantitative analysis using sine waves

The SVD analysis shows that an non-linear appearance manifold can be smoothed using a low-pass filter. One can thus sample inside a locally-linear region and compute a linear approximation of the filtered manifold. In this section, we present a quantitative analysis of sampling and estimating motion on the smoothed manifold. In particular, for a given sampling density (camera baseline), we try to determine the threshold frequency for the low-pass filter and derive an estimate of the estimation error. In the analysis, we use sine signals as the scene contents, for any image can be decomposed into a series of sine waves of different frequencies.
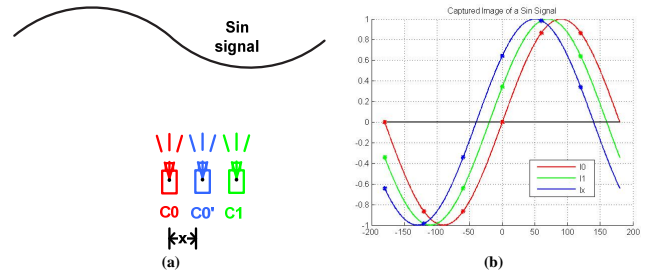

Figure 3. 1D orthographic cameras capture images of a sine signal.

Without loss of generality, let us consider the problem in one dimension. Suppose two parallel 1D orthographic cameras C_0 and C_1 capture images I_0 and I_1 of a sine signal as shown in Fig. 3(a). Both images contain r samples from one period of the sine signal, starting from initial phases a_0 and a_1 as shown in Fig. 3(b). At the next frame, C_0 moves x degrees along the wave and captures a new image I_x at initial phase $a_x = a_0 + x$. We can write the 1D images as:

$$I_j = sin(a_j + r\, k) \tag{7}$$

where $j \in [0, 1, x]$ and $k \in [0, 1, \ldots, \lfloor 359/r \rfloor]$. Using Equation (5) and (6), we compute a linear estimate of the motion $\tilde{x}$ as:

$$\tilde{x} = (a_1 - a_0)\,(I_x - I_0)/(I_1 - I_0) \tag{8}$$

The estimation errors for different motions x using different baselines are shown in Fig. 4. One can see from Fig. 4(a) that with two cameras of baseline $b = a1 - a0$, the estimation error remains relatively small for motion within $[0, b]$ and increases quickly beyond this region. Region $[0, b]$ is the linear region for motion estimation. Fig. 4 (b) shows that while using a bigger baseline enlarges the linear region, it also causes greater estimation errors for motions within the linear range. For instance, using a baseline $b = 120$ the estimation error for $x = 30$ is 5 degrees. In practice, we empirically choose $b = 90$ to achieve a balance between the size of tracking volume and the tracking accuracy. This

means for a particular scene, we can consider adjusting the camera baseline to be a quarter of highest frequency in the image. Or for a fixed baseline, we should use a low-pass filter whose threshold is four times the camera baseline. Then we can expect to achieve good estimation for a motion within the baseline.
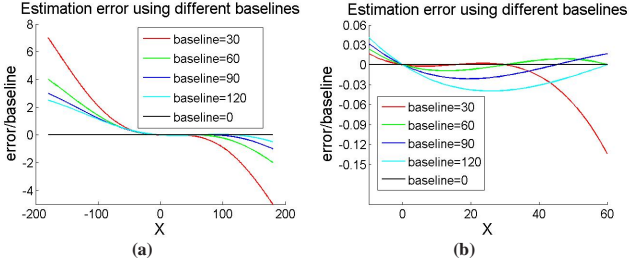

Figure 4. Analysis of motion estimation error. (a) Estimation error $(\tilde{x}-x)/b$ using specific baselines $b = a1 - a0 = [30, 60, 90, 120]$ degrees, and $x \in [-180, 180]$ degrees. (b) Zoom in of (a) for $x \in [-10, 60]$ degrees.

We have derived some interesting conclusions using analysis on 1D orthogonal cameras observing sine signals. Unfortunately, the analysis can not be directly extended to 3D scenes and perspective cameras. Here we provide some empirical verification. Consider the synthetic data set used in the previous section. The shift of a point in the image plane is in $[0, 4]$. According to the previous analysis, the wave length of the highest frequency should be 16 pixels. That is a 40 Hz signal for a 640×640 image. From Fig. 2(c) and Table 1, we can see that 95% energy of a Gaussian filter with $\sigma = 6$ is covered by its low-frequency spectrum inside $[-40, 40]$. Thus the threshold of this low-pass filter is 40Hz. Whereas for the filter with $\sigma = 3$, only 59% energy is within the 40Hz low-frequency spectrum. As shown in Fig. 2(d,e), a good linear approximation can be computed for images blurred with the first filter but not for the second one. The results support the analysis.

Gaussian kernel σ	3	6	12
Percentage energy covered by the low frequency spectrums [-40,40]	59%	96%	99%

Table 1. Energy distribution of Gaussian filters in the frequency domain.

The above analysis shows that the appropriate tracking volume is $[0, b]$, which means the estimation error is asymmetric. To solve this problem, one can consider choosing the center camera according to the motion direction. For instance, in the 1D case, if the cameras move to the left (see Fig. 3), we can choose C_1 to be the center camera and use I_0 and I_1 captured at the new frame to compute intensity derivatives. This solution can be extended to 3D cases. To use this technique, we need to detect the direction of the motion. This can be achieved by doing motion estimating twice, first for the direction and then for the real estimation. While this solution appears to be awkward, the additional computation is affordable, as it only involves solving a linear system that can be done efficiently.

5. Experimental Results

We first present some results based on synthetic data. We simulated a scene consisting of a textured planar patch and a curved mirror, both contained inside an a cube. The inner six surfaces of the (surrounding) cube were textured using the same image. The simulated camera cluster was placed in front of the curved mirror. Thus the camera cluster viewed some of the scene beyond the edges of the mirror, and some of the reflection. Traditional tracking techniques would not perform well on this data, since the epipolar constraint does not hold for images of the curved mirror as the camera moves.

Fig. 5 presents some tracking results on the synthetic scene over 40 frames. An original image (640×640) is shown in (a), where the border of the curved mirror is marked in green. One can see that the reflection of the planar patch is distorted by the curved mirror. When generating the image sequences, we restricted the maximum extent of the camera motion so that the pixel motion for frontal scene points would be less than 4 pixels. We generated a blurred image (shown in (e)) using a Gaussian kernel of 160×160 with $\sigma = 24$ and sub-sampled at 32 Hz (20 pixels). We choose a σ that was larger than the analysis result shown in 4.2 to accommodate the reflection of the rear scene, which could move faster in the image plane than the front scene. We show the translation and rotation estimates in Fig. 5 (b-d) and (f-h). The horizontal axes represent frame numbers and the vertical axes represent the accumulated motion across the previous frames. In the plots, the red curves represent the true value, and blue curves represent the estimated value. The translation and rotation of the camera is defined in a global coordinate system that is aligned with the coordinate system of the center camera at the initial frame.

In a second experiment, we tracked a real camera cluster. The cluster was built using four PointGrey Flea digital color cameras (see Fig. 1). The baselines are 34 mm in the X and Y direction, and 66 mm in the Z direction. As described in 3, geometric and photometric consistencies were enforced across the four cameras. The color images were converted to grayscale and used as scene appearance samples.

To obtain some form of a ground-truth reference motion track we moved the camera cluster along some predetermined grid points marked on a table (the X-Z plane) while imaging the scene. Prior to data collection the cameras were manually adjusted to obtain parallel principal axes across frames. The results are shown in Fig. 6. An original image and its blurred version is shown in (a) and

(e). The resolution of the original image is 1024×768. The image was blurred using a Gaussian kernel of 160×160 with $\sigma = 24$, and then sub-sampled at a ratio of 20 to 1. The accumulated translations and rotations are shown in (b-d) and (f-h). Again, the translations and rotations are defined in the coordinate of the center camera at the initial frame. One can see that the algorithm achieves good estimation on X and Y translations, and the estimated rotations and Z translations are small. We believe the exhibited error is due primarily to inherent error in our (incremental) approach, and registration error introduced by our manual alignment process.

Our third experiment demonstrates the tracking of a hand-held camera cluster over 200 frames. As the ground truth motion was unknown, we illustrate the tracking accuracy using projection error. Six 3D scene points were chosen, and the coordinates of their projections in the four images of the initial frame were extracted using a standard OpenCV KLT tracker. We then back-projected and computed their 3D positions in the world coordinates defined by the pose of the center camera at the first frame. As the cluster moved, its incremental motion at every frame was estimated and the accumulated motion between the current frame and the first frame was computed. These accumulated motion parameters were then used to compute a projection matrix of the center camera at its current pose. We used the estimated projection matrix to project the 3D points onto the current *center* image, and indicated the projections with white patches. The results are presented in Fig. 7. The images are blurred and sub-sampled using the same parameters described in the second experiment. (a) shows the projections of the 3D points in the *center* image at the initial frame. The projections using matrices computed by estimated camera motions are shown in (b-h).

6. Conclusions

We presented a novel method for incrementally tracking camera motion through sampling and linearizing the local appearance manifold. We have demonstrated the method using both simulation and a real prototype camera cluster.

One area of future work we envision is related to the imaging component of the cluster. We have some ideas for using custom optics to effectively achieve the same center, translational, and rotational images using a *single* image sensor. This could make the unit more compact, while also helping address color, geometry, and speed issues.

In addition, the relatively simple and regular nature of the computation could lead to a relatively fast system for on-line estimation, perhaps using specialized embedded hardware such as FPGAs. As the processing speed increases, the inter-frame time could be decreased, improving the linear approximations and some other aspects of the approach.

Finally, because the method is inherently incremental (estimating and integrating dP), it is likely that in practice one would want to periodically use some of the images for more conventional feature-based drift correction. Like MPEG and other video encoding schemes, future hardware could send a continuous dP stream with periodic key frames to the host computer, enabling fast incremental tracking with drift estimation and correction.

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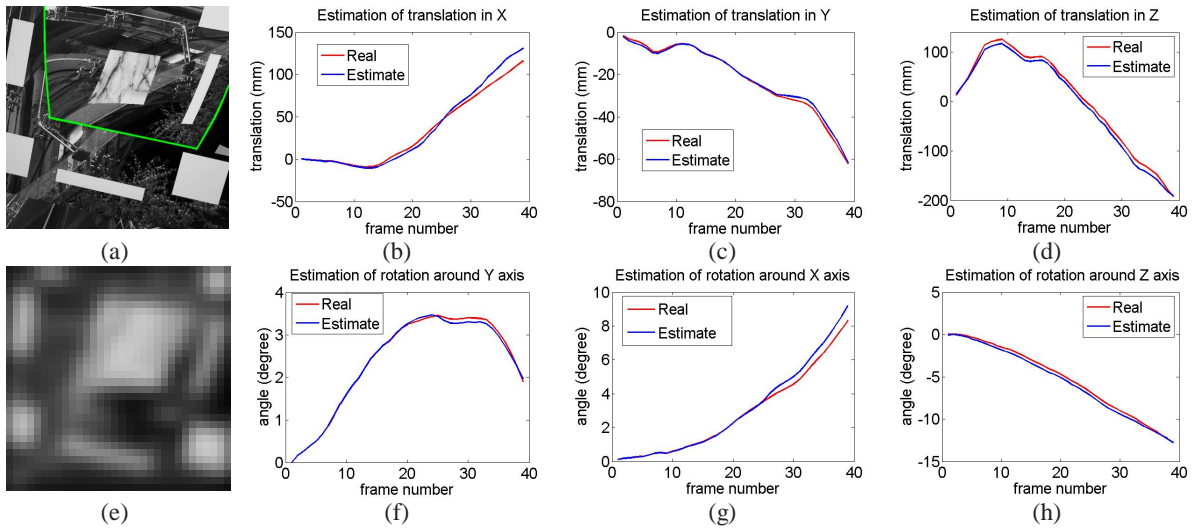
Figure 5. Tracking in a synthetic scene with a curved mirror over 40 frames. (a) An image of the synthetic scene. The border of the curved mirror is marked in green. (b)-(d) Estimation of camera translations (in mm) in X, Y and Z directions. Red curves represent the true value of the accumulated motion, blue curves represent the estimated value of the accumulated motion. (e) A blurred image. (f)-(h) Estimation of camera rotation angles (in degree) around Z, X and Y axes. Red curves represent the true values of the accumulated motion, blue curves represent the estimated values of the accumulated motion.
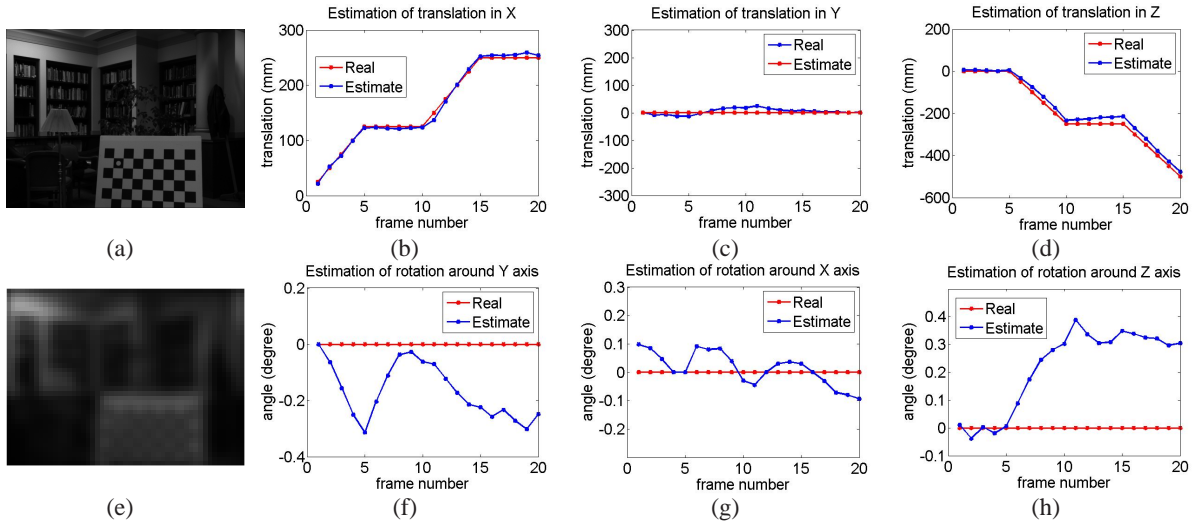

Figure 6. Tracking a controlled camera motion over 20 frames. (a) A image of the real scene. (b)-(d) Estimation of camera translations (in mm) in X, Y and Z directions. Red curves represent the true values of the accumulated motion, blue curves represent the estimated values of the accumulated motion. (e) A blurred image. (f)-(h) Estimation of camera rotation angles (in degree) around Z, X and Y axes. Red curves represent the true values of the accumulated motion, blue curves represent the estimated values of the accumulated motion.
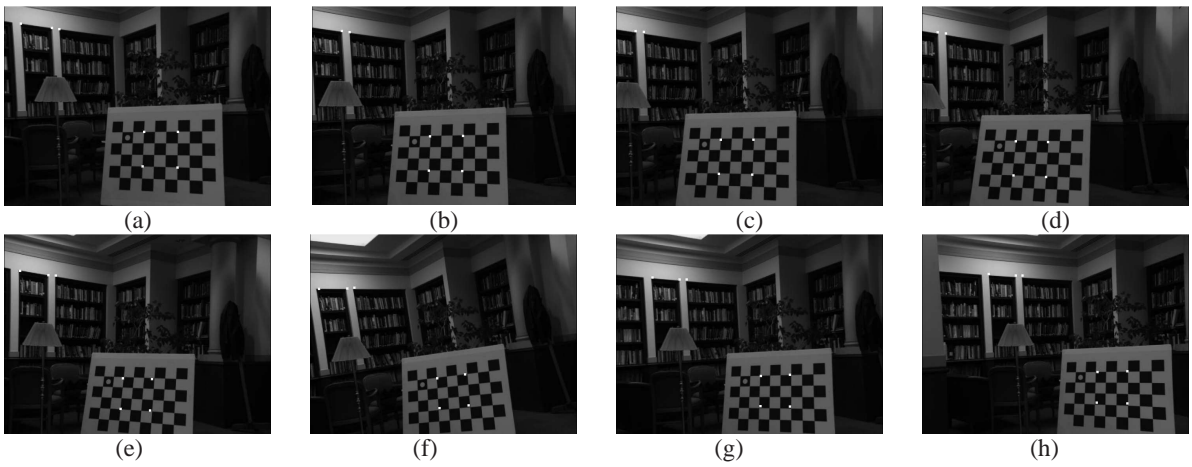
Figure 7. Tracking a hand-held camera motion over 200 frames. The tracking results are illustrated through projecting six 3D scene points onto the image plane. The projection matrix is computed using the estimated motion. The positions of the 3D points are marked as white patches. (a) The projected points in the *center* image at the initial frame. (b)-(h) The projected points in the *center* image at frame 20, 40, 60, 140, 160, 180 and 200.